Advanced Algebra
Homework 7.1
Explicit Rules for Sequences

Name $\qquad$

Period $\qquad$

## SHOW ALL WORK.

Complete Parts A \& B OR Parts B \& C

## PART A:

Determine whether the given sequence is Arithmetic, Geometric, or Neither. Explain why.

1. $5,14,23,32,41, \ldots$
2. $16,14,11,6,3, \ldots$
3. $216,36,6,1, \frac{1}{6}, \ldots$
4. $4,16,64,256,1024, \ldots$
5. $1,-2,-5,-8,-11, \ldots$
6. $1,4,8,16,32, \ldots$

Write a rule for the $n$th term of the sequence. Then find $\mathbf{a}_{20}$.
7. $1,4,7,10,13, \ldots$
8. $5,11,17,23,29, \ldots$
9. $8,21,34,47,60, \ldots$

Write a rule for the nth term of the sequence. Then find $\mathbf{a}_{7}$.
10. $1,-4,16,-64, \ldots$
11. $6,18,54,162, \ldots$
12. $4,24,144,864, \ldots$

## PART B:

Determine whether the given sequence is Arithmetic, Geometric, or Neither. Explain why.
13. $-10,-7,-5,-2,0, \ldots$
14. $0.5,1,1.5,2,2.5, \ldots$
15. $20,10,5,2.5,1.25, \ldots$
16. $\frac{1}{3}, \frac{2}{3}, \frac{4}{3}, \frac{8}{3}, \ldots$
17. $\frac{1}{2}, 1, \frac{3}{2}, 2, \frac{5}{2}, \ldots$
18. $-\frac{1}{4}, \frac{3}{8},-\frac{3}{16}, \frac{1}{32},-\frac{3}{64}, \ldots$

Write a rule for the $n$th term of the sequence. Then find $\mathbf{a}_{20}$.
19. $-3,-1,1,3,5, \ldots$
20. $6,2,-2,-6,-10, \ldots$
21. $25,14,3,-8,-19, \ldots$

Write a rule for the $n$th term of the sequence. Then find $\mathbf{a}_{7}$.
22. $7,-35,175,-875, \ldots$
23. $2, \frac{3}{2}, \frac{9}{8}, \frac{27}{32}, \ldots$
24. $3,-\frac{6}{5}, \frac{12}{25},-\frac{24}{125}, \ldots$

Write an explicit rule for the $n$th term of the sequence.
25. $a_{16}=52 ; d=5$
26. $a_{6}=-16 ; d=9$
27. $a_{4}=96 ; d=-14$
28. $a_{1}=5 ; r=3$
29. $a_{1}=-2 ; r=6$
30. $\mathrm{a}_{2}=6 ; \mathrm{r}=2$
31. Describe and correct the error in writing the explicit rule for the nth term in the arithmetic sequence $37,24,11,-2, \ldots$
$a_{1}=37, d=-13$.
$\mathrm{a}_{\mathrm{n}}=-13+(\mathrm{n}-1)(37)$
$a_{n}=-50+37 n$
32. In a skydiving formation with $R$ rings, each ring after the first ring has twice as many skydivers as the preceding ring. The formation for $\mathrm{R}=2$ is shown.
a. Let $a_{n}$ be the number of skydivers in the $n$th ring. Find a rule for $a_{n}$.

b. Find the total number of skydivers if there are 4 rings.
33. A marching band is arranged in 7 rows. The first row has 3 band members, and each row after the first row has 2 more band members than the row before it. Write an explicit rule for the number of band members in the nth row. Then find the total number of band members.

## PART C:

Determine whether the given sequence is Arithmetic, Geometric, or Neither. Explain why.
34. $\frac{7}{4}, \frac{5}{4}, \frac{3}{4},-\frac{3}{4},-\frac{5}{4}, \ldots$
35. $0.75 .1 .5,2.25,3,3.75, \ldots$
36. $-\frac{5}{2},-1, \frac{1}{2}, 2, \frac{7}{2}, \ldots$

Write a rule for the $n t h$ term of the sequence. Then find $\mathbf{a}_{20}$.
37. $0, \frac{2}{3}, \frac{4}{3}, 2, \ldots$
38. $2, \frac{5}{3}, \frac{4}{3}, 1, \ldots$
39. $1.5,3.6,5.7,7.8, \ldots$

Write a rule for the nth term of the sequence. Then find $a_{7}$.
40. $7,-4.2,2.52,-1.512, \ldots$
41. $5,-14,39.2,-109.76, \ldots$
42. $120,180,270,405, \ldots$

Write an explicit rule for the nth term of the arithmetic sequence.
43. $\mathrm{a}_{4}=31 ; \mathrm{a}_{10}=85$
44. $\mathrm{a}_{6}=39 ; \mathrm{a}_{14}=79$
45. $a_{3}=-2 ; a_{17}=40$
46. During a high school spirit week, students dress up in costumes. A cash prize is given each day to the student with the best costume. The organizing committee has $\$ 1000$ to give away over 5 days. The committee wants to increase the amount of the prize by $\$ 50$ each day. How much should the committee give away on the first day?
47. A theater has $n$ rows of seats, and each row has $d$ more seats than the row in front of it. There are $x$ seats in the last (nth) row and a total number of $y$ seats in the entire theater. How many seats are there in the front row? Write your answer in terms of $\mathrm{n}, \mathrm{x}$, and y .
48. On January 1 of each year, you deposit $\$ 2000$ in an individual retirement account (IRA) that pays $5 \%$ annual interest. You make a total of 30 deposits. How much money do you have in your IRA immediately after you make your last deposit?

